

## A NEW SU(5) MODEL

J. RIZOS and K. TAMVAKIS

*Physics Department, University of Ioannina, GR-451 10 Ioannina, Greece*

Received 11 April 1988

The standard matter-fermions and Higgses of the 27 representation of  $E_6$  can be put in SU(5) representations in three distinct ways yielding, the Georgi-Glashow SU(5), the recently revived, and superstring related, flipped SU(5)  $\times$  U(1)<sub>X</sub> model, and a new, possibly superstring related, SU(5)  $\times$  U(1)<sub>X</sub>  $\times$  U(1)<sub>D</sub> model with unique features. The gauge symmetry is broken down to SU(3)<sub>c</sub>  $\times$  SU(2)<sub>L</sub>  $\times$  U(1)<sub>Y</sub> with Higgses in the  $10 + \bar{10} + 1 + \bar{1}$  representation of SU(5). The model exhibits a natural triplet-doublet splitting. Neutrinos can obtain a phenomenologically acceptable radiative Dirac mass.

While the number of compactified and four-dimensional string theories [1,2,3] is increasing, it is still difficult to single out a string theory, and a related to it gauge field theory, that has the desired phenomenological properties. In the recent superstring inspired GUT literature however, new models such as the flipped SU(5)  $\times$  U(1) GUT [4,5] have appeared with unique features interesting in themselves. For example, a common property of the observable sector in field theory models that result from superstrings is the absence of any adjoint Higgses. Another feature is the appearance of extra U(1) gauge group factors [6]. These features have initiated efforts starting from the beginning and constructing new GUT models with these properties that may be obtainable from a string theory. The purpose of this article is to construct and analyze a new adjointless  $N=1$  supersymmetric SU(5) model which exhibits some unique and interesting properties.

It is a common fact that the standard fermions and Higgses can be accommodated in the 27 representation of  $E_6$  together with the right-handed neutrino, an additional pair of down-quarks and an additional singlet. Under the maximal subgroup SO(10)  $\times$  U(1)<sub>D</sub> the 27 is decomposed as

$$27 = (16, 1) + (10, -2) + (1, 4). \quad (1)$$

Further, under the maximal subgroup SU(5)  $\times$  U(1)<sub>X</sub> of SO(10), these representations are decomposed as

$$27 = [ (10, -1, 1) + (\bar{5}, 3, 1) + (1, -5, 1) ] \\ + [ (\bar{5}, -2, -2) + (5, 2, -2) ] + [ (1, 0, 4) ]. \quad (2)$$

In SU(5)  $\times$  U(1)<sub>X</sub>  $\times$  U(1)<sub>D</sub> there exist three distinct ways to define the hypercharge and obtain the correct assignments for the standard fermions and Higgses. The simplest case is that of the Georgi-Glashow SU(5) in which U(1)<sub>X</sub>  $\times$  U(1)<sub>D</sub> does not contribute to the hypercharge and U(1)<sub>Y</sub> is contained entirely in SU(5). The second distinct possibility is that of the "flipped" SU(5)  $\times$  U(1)<sub>X</sub> in which U(1)<sub>Y</sub> is a combination of U(1)<sub>X</sub> and a U(1)<sub>Z</sub> subgroup of SU(5). There is however a third possibility in which both U(1)<sub>X</sub> and U(1)<sub>D</sub> participate in the definition of the hypercharge. In that case one gets a new SU(5)  $\times$  U(1)<sub>X</sub>  $\times$  U(1)<sub>D</sub> model quite different from the previous cases. In order to compare the differences of the three models it is worthwhile listing the field content of the matter representations in the three cases

$$(i) Y = \frac{1}{6} Z \text{ (Georgi-Glashow SU(5))}: \\ (10, -1, 1) = \begin{pmatrix} Q \\ U^c E^c \end{pmatrix}, \quad (\bar{5}, 3, 1) = \begin{pmatrix} D^c \\ L \end{pmatrix}, \\ (1, -5, 1) = N^c, \quad (\bar{5}, -2, -2) = \begin{pmatrix} B^c \\ H \end{pmatrix}, \\ (5, 2, -2) = \begin{pmatrix} B \\ H^c \end{pmatrix}, \quad (1, 0, 4) = N. \quad (3)$$

(ii)  $Y = -\frac{1}{3}X - \frac{1}{30}Z$  (flipped SU(5)):

$$\begin{aligned}
 (10, -1, 1) &= \begin{pmatrix} Q \\ D^c N^c \end{pmatrix}, & (\bar{5}, 3, 1) &= \begin{pmatrix} U^c \\ L \end{pmatrix}, \\
 (1, -5, 1) &= E^c, & (\bar{5}, -2, -2) &= \begin{pmatrix} B^c \\ H \end{pmatrix}, \\
 (5, 2, -2) &= \begin{pmatrix} B \\ H \end{pmatrix}, & (1, 0, 4) &= N.
 \end{aligned} \quad (4)$$

(iii)  $Y = \frac{1}{3}\Omega + \frac{1}{30}X - \frac{1}{30}Z$  (doubly-flipped SU(5)):

$$\begin{aligned}
 \mathcal{Q}(10, -1, 1) &= \begin{pmatrix} Q \\ B^c N \end{pmatrix}, & \mathcal{D}^c(\bar{5}, 3, 1) &= \begin{pmatrix} D^c \\ H^c \end{pmatrix}, \\
 \mathcal{N}^c(1, -5, 1) &= N^c, & \mathcal{U}^c(\bar{5}, -2, -2) &= \begin{pmatrix} U^c \\ H \end{pmatrix}, \\
 \mathcal{L}(\bar{5}, 2, -2) &= \begin{pmatrix} B \\ L \end{pmatrix}, & \mathcal{E}^c(1, 0, 4) &= E^c.
 \end{aligned} \quad (5)$$

We have denoted with  $Z$  the U(1) generator belonging to SU(5). The quantum number assignments of the eleven Q, B<sup>c</sup>... fields are listed in table 1.

It is evident that the SU(5) × U(1)<sub>X</sub> × U(1)<sub>Ω</sub> model is distinct from flipped SU(5) since the SU(3)<sub>C</sub> × SU(2)<sub>L</sub> × U(1)<sub>Y</sub> content of 5's is different. The allowed flippings B<sup>c</sup> ↔ D<sup>c</sup>, L ↔ H, N ↔ N<sup>c</sup> do not alter the fact that colour triplets of charge  $\frac{1}{3}$  are together with hypercharge + $\frac{1}{3}$  isodoublets. The model is characterized by some unique features.

(i) Left-handed leptons and right-handed up-quarks belong to the 10 representation of SO(10).

(ii) The right-handed electron is an SO(10) singlet.

(iii) Left-handed quarks, right-handed down-quarks and right-handed neutrinos belong to the 16 representation of SO(10) as usually.

(iv) Higgs isodoublets of hypercharge + $\frac{1}{2}$  belong to the 16 representation while those of hypercharge - $\frac{1}{2}$  belong to the 10 representation.

The superfield content of a supersymmetric SU(5) × U(1)<sub>X</sub> × U(1)<sub>Ω</sub> GUT except the gauge vector supermultiplet includes  $N_F$  chiral matter superfields  $\mathcal{Q}, \mathcal{D}^c, \mathcal{N}^c, \mathcal{U}^c, \mathcal{L}, \mathcal{E}^c$  with the quantum number assignments shown in (5). These are exactly the building blocks of  $N_F$  copies of the 27 representation of E<sub>6</sub>. In addition we introduce two pairs of massless Higgs chiral superfields in the (10, -1, 1) + (10̄, 1, -1) and in the (1, -5, 1) + (1̄, 5, -1) representations

$$\begin{aligned}
 &\mathcal{Z}_H(10, -1, 1) + \bar{\mathcal{Z}}_H(\bar{10}, 1, -1) \\
 &= \begin{pmatrix} Q_H \\ B_H^c N_H \end{pmatrix} + \begin{pmatrix} \bar{Q}_H \\ \bar{B}_H^c \bar{N}_H \end{pmatrix}, \\
 &\mathcal{N}_H^c(1, -5, 1) + \bar{\mathcal{N}}_H^c(1, 5, -1) = N_H + \bar{N}_H,
 \end{aligned} \quad (6)$$

whose expectation value in the D-flat direction  $\langle N_H \rangle = \langle \bar{N}_H \rangle$ ,  $\langle N_H^c \rangle = \langle \bar{N}_H^c \rangle$  breaks SU(5) × U(1)<sub>X</sub> × U(1)<sub>Ω</sub> to SU(3)<sub>C</sub> × SU(2)<sub>L</sub> × U(1)<sub>Y</sub><sup>21</sup>. Q<sub>H</sub>,

<sup>21</sup> The absence of the vacuum expectation value  $\langle N_H^c \rangle = \langle \bar{N}_H^c \rangle$  would result in an SU(3)<sub>C</sub> × SU(2)<sub>L</sub> × U(1)<sub>Y</sub> × U(1)<sub>ψ</sub> model, characterized by an additional light neutral gauge boson.

Table 1  
U(1) quantum numbers of matter particles in SU(5) models.

SU(3) <sub>C</sub> × SU(2) <sub>L</sub> × U(1) <sub>Y</sub>	SU(5)			SU(5) × U(1) <sub>X</sub>			SU(5) × U(1) <sub>X</sub> × U(1) <sub>Ω</sub>		
	Z	X	Ω	Z	X	Ω	Z	X	Ω
Q(3, 2, $\frac{1}{6}$ )	1	-1	1	1	-1	1	1	-1	1
D <sup>c</sup> ( $\bar{3}$ , 1, $\frac{1}{3}$ )	2	3	1	-4	-1	1	2	3	1
U <sup>c</sup> ( $\bar{3}$ , 1, - $\frac{2}{3}$ )	-4	-1	1	2	3	1	2	-2	-2
L(1, 2, - $\frac{1}{2}$ )	-3	3	1	-3	3	1	3	2	-2
E <sup>c</sup> (1, 1, 1)	6	-1	1	0	-5	1	0	0	4
N <sup>c</sup> (1, 1, 0)	0	-5	1	6	-1	1	0	-5	1
H(1, 2, - $\frac{1}{2}$ )	-3	-2	-2	3	2	-2	-3	-2	-2
H <sup>c</sup> (1, 2, $\frac{1}{2}$ )	3	2	-2	-3	-2	-2	-3	3	1
B(3, 1, - $\frac{1}{3}$ )	-2	2	-2	-2	2	-2	-2	2	-2
B <sup>c</sup> ( $\bar{3}$ , 1, $\frac{1}{3}$ )	2	-2	-2	2	-2	-2	-4	-1	1
N(1, 1, 0)	0	0	4	0	0	4	6	-1	1

$\bar{Q}_H$  and two singlets, linear combinations of  $N_H$ ,  $\bar{N}_H$ ,  $N_H^c$  and  $\bar{N}_H^c$ , are absorbed while  $B_H^c$  and  $\bar{B}_H^c$  and two other combinations of singlets are left-over.

Consider now the cubic superpotential <sup>42</sup>

$$W_0 = g_{ijk}(u, d) \mathcal{L}_i \mathcal{L}_j^c \mathcal{W}_k^c + g_{ijk}(v) \mathcal{L}_i \mathcal{L}_j^c \mathcal{N}_k^c + g_{ijk}(e) \mathcal{L}_i \mathcal{W}_j^c \mathcal{E}_k^c + g_{ij}(H) \mathcal{L}_i \mathcal{L}_j \mathcal{L}_k^c \quad (7)$$

The first term of (7)

$$g(u, d) (QD^c H + QU^c H^c + B^c D^c U^c + NHH^c) \quad (8)$$

is responsible for up- and down-quark masses. The fact that both up- and down-quark masses result from a common coupling is a unique feature of this model not shared by the other SU(5) models.

The second term of the superpotential (7)

$$g(v) (LN^c H^c + D^c N^c B) \quad (9)$$

is responsible for the neutrino Dirac mass. The fact that the Yukawa coupling responsible for the neutrino Dirac mass is independent from the other Yukawa couplings makes it technically possible, although not necessarily appealing, to have Dirac neutrinos light as required by phenomenology by adjusting  $g(v)$  to a small value. We shall come back later to the problem of the neutrino mass and shown how it can be naturally solved through a modification of the model.

The third term in (7)

$$g(e) (LHE^c + BU^c E^c) \quad (10)$$

is responsible for charged lepton masses.

Finally, the last term

$$g(H) (QQ_H B + QB_H^c L + B^c Q_H L + B^c N_H B + NB_H^c B) \quad (11)$$

leads to a superheavy mass for the B and B<sup>c</sup> fields

$$g_{ij}(H) \langle N_H \rangle B_i^c B_j. \quad (12)$$

Thus all baryon number violating couplings present in (8), (9) and (10) become harmless due to the supermassiveness of B and B<sup>c</sup>. Apart from the not very crucial terms  $\mathcal{L}\mathcal{L}\mathcal{L}$  and  $\mathcal{L}_H \mathcal{L}_H \mathcal{L}$ , the discrete symmetry imposed forbids a dangerous term  $\mathcal{L}_H \mathcal{L}^c \mathcal{W}^c$  which contains a superheavy mass  $\langle N_H \rangle H_i H_j^c$  for the Higgs

isodoublets. This term would spoil the lightness of the Higgs isodoublets. It is also the main obstacle to a straightforward extension of the present model to an SO(10) × U(1)<sub>G</sub> GUT.

The model as it stands, below  $\langle N_H \rangle = \langle \bar{N}_H \rangle \approx \langle N_H^c \rangle = \langle \bar{N}_H^c \rangle \approx M_X$  contains  $N_F$  quarks and leptons as well as  $N_F$  pairs of Higgs isodoublets. In addition, except the two Higgs singlets, it contains  $N_F$  massless singlets  $N_i$  and one pair of massless colour triplets  $B_H^c$  and  $\bar{B}_H^c$ . Masses for this additional set of fields would be absent even when supersymmetry is broken unless we consider new interactions. These could arise either from a gauge singlet sector or a massive Higgs sector. The model can be extended to include  $N_F$  massive gauge singlet superfields  $\Phi_i(1, 0, 0)$  and two pairs of massive superfields <sup>43</sup>

$$\mathcal{D}_H^c(\bar{5}, 3, 1) + \bar{\mathcal{D}}_H^c(5, -3, -1) + \mathcal{W}_H^c(\bar{5}, -2, -2) + \bar{\mathcal{W}}_H(5, 2, 2)$$

The superpotential now will include the terms <sup>44</sup>

$$W_1 = f_{ij} \mathcal{L}_i \mathcal{L}_j \bar{\mathcal{D}}_H \Phi + \lambda_i \mathcal{L}_i \mathcal{D}_H \mathcal{W}_i^c + \lambda' \bar{\mathcal{L}}_H \bar{\mathcal{D}}_H \bar{\mathcal{W}}_H + \lambda'_i \mathcal{L}_i \mathcal{D}_H \mathcal{W}_i^c + \lambda''_i \mathcal{L}_i \mathcal{D}_H \mathcal{W}_i^c + g_i \Phi_i \mathcal{D}_H \bar{\mathcal{D}}_H + g'_i \Phi_i \mathcal{W}_H^c \bar{\mathcal{W}}_H + f_{ijk} \Phi_i \Phi_j \Phi_k + M_{ij} \Phi_i \Phi_j + M(\mathcal{D}_H \bar{\mathcal{D}}_H + \mathcal{W}_H^c \bar{\mathcal{W}}_H). \quad (13)$$

The first term in (13)

$$f(B^c \bar{B}_H^c \Phi + Q \bar{Q}_H \Phi + N \bar{N}_H \Phi) \quad (14)$$

provides us with a Dirac mass term  $f_{ij} \langle \bar{N}_H \rangle N_i \Phi_j$  which combines with the term  $M_{ij} \Phi_i \Phi_j$  and gives masses of order  $M_X^2/M$  for  $N_i$  <sup>45</sup>.

Another important function of the same coupling is that it can generate through radiative corrections masses for the  $B_H^c$  and  $\bar{B}_H^c$  fields as shown in fig. 1. A lower mass limit on this mass is imposed from the, in general, family changing coupling  $Q_L B_H^c$  that can induce operators  $b\nu\bar{u}\bar{e}$ ,  $t\bar{e}\bar{u}\bar{u}$ , etc. with interesting phenomenological signatures.

<sup>43</sup> Note that all fields belong to complete or incomplete  $\bar{27}$  and  $\bar{27}$  resp. of E<sub>6</sub>.

<sup>44</sup> The trilinear part is the most general under the extension of the first Z<sub>2</sub> discrete symmetry  $\mathcal{D}_H \rightarrow -\mathcal{D}_H, \bar{\mathcal{D}}_H \rightarrow -\bar{\mathcal{D}}_H$ .

<sup>45</sup> It is natural to assume that  $M, M_{ij}$  are of the order of the Planck mass i.e.  $O(10^{18}$  GeV). Similarly, couplings to extra singlets  $\chi, \mathcal{L}_H \mathcal{L}_H \chi^c, \mathcal{L}_H \mathcal{L}_H \mathcal{N}_H^c$  can render the surviving Higgs singlets in  $\mathcal{L}_H, \bar{\mathcal{L}}_H, \mathcal{N}_H^c$  and  $\bar{\mathcal{N}}_H^c$  massive.

<sup>42</sup> This is the most general under the discrete Z<sub>2</sub> × Z<sub>2</sub> symmetry  $\mathcal{L}_H \rightarrow \mathcal{L}_H, \mathcal{W}_H^c \rightarrow -\mathcal{W}_H^c, \mathcal{L}_H^c \rightarrow -\mathcal{L}_H^c, \mathcal{N}_H^c \rightarrow -\mathcal{N}_H^c, \bar{\mathcal{L}}_H \rightarrow -\bar{\mathcal{L}}_H, \bar{\mathcal{W}}_H \rightarrow -\bar{\mathcal{W}}_H, \bar{\mathcal{N}}_H \rightarrow -\bar{\mathcal{N}}_H$ .

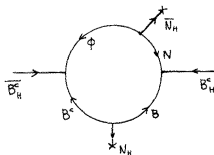


Fig. 1. Radiative mass of  $B_{H_1}$  and  $\tilde{B}_{H_1}$ .

The other terms in (13), apart from the irrelevant  $B_{H_1} D_{H_1}^c U^c$ ,  $\tilde{B}_{H_1} D^c U_{H_1}^c$ ,  $\tilde{B}_{H_1} \tilde{D}_{H_1}^c U_{H_1}^c$ ,  $Q D_{H_1}^c H_{H_1}$ , ... etc, include

$$\lambda_i \langle N_H \rangle H_i H_{H_1} + \lambda'_i \langle N_H \rangle H_i^c H_{H_1} + \tilde{\lambda} \langle \tilde{N}_H \rangle \tilde{H}_{H_1} \tilde{H}_H + M (H_{H_1} \tilde{H}_{H_1} + H_H \tilde{H}_H). \quad (15)$$

Thus, one combination, namely  $\lambda_i H_i$  and  $\lambda'_i H_i^c$  of Higgs isodoublets become massive of an intermediate mass. This is evident from the Higgs isodoublet mass matrix which is (roughly)

$$\begin{pmatrix} 0 & M'_X & 0 \\ M_X & 0 & M \\ 0 & M & M'_X \end{pmatrix} \quad (16)$$

in a  $\lambda_i H_i$ ,  $H_H$ ,  $\tilde{H}_{H_1}$  and  $\lambda'_i H_i^c$ ,  $H_H^c$ ,  $\tilde{H}_{H_1}^c$  basis. The eigenvalues of the mass matrix (16) are approximately

$$M, -M, O(M_X^2/M^2). \quad (17)$$

It is important that the introduced couplings to the massive Higgses make one combination of Higgs isodoublets heavy. To many light Higgs isodoublets destroy the predicted value of the electroweak mixing angle.

As we mentioned previously, neutrinos can obtain a direct Dirac mass from the coupling  $g(\nu)LH^c N^c$  which is unrelated to any other Yukawa coupling and therefore it would be technically possible to adjust it to a phenomenologically acceptable value. Nevertheless this is not theoretically satisfactory. It is possible to have the standard neutrino mass term  $\mathcal{L}^{\mathcal{D}^c N^c}$  forbidden, and therefore the direct neutrino mass term absent, due to the properties of  $\mathcal{N}^c$  under the imposed discrete symmetry. Thus, if we had  $\mathcal{N}^c \rightarrow \mathcal{N}^c$ ,  $\tilde{\mathcal{N}}^c \rightarrow -\tilde{\mathcal{N}}^c$ , under  $Z_2$ , no tree-level neutrino mass is present. However, the neutrino field would still be

able to couple to  $\mathcal{L}$  through the, now allowed, term  $\mathcal{L}^{\mathcal{D}^c H^c N^c} = LH_{H_1}^c N^c + BD_{H_1}^c N^c$ . No vacuum expectation value for  $H_{H_1}^c$  is possible since it is superheavy and consequently still no tree-level mass for the neutrino is present. Nevertheless, radiative corrections through the diagrams shown in fig. 2 generate a naturally small neutrino Dirac mass in agreement with phenomenology [7].

The model as it stands now contains  $N_F$  light families of quarks and leptons, and pair of light  $B_{H_1}$  and  $\tilde{B}_{H_1}$ ,  $(N_F - 1)$  pairs of light Higgs isodoublets and one pair of intermediate-mass Higgs isodoublets. The rest of the fields are massive below  $M_X$ . The renormalization group analysis of the model gives  $\sin^2 \theta_W$  in agreement with current experimental values for a range of values of the parameter

$$\tilde{\alpha} = [\frac{3}{20} \alpha_F^{-1} (M_X) + \frac{2}{3} \alpha_D^{-1} (M_X)]^{-1}, \quad (18)$$

where  $\alpha_F$  and  $\alpha_D$  are the couplings of the normalized<sup>86</sup>  $U(1)_F$  and  $U(1)_D$ . The values obtained for  $N_F = 3$  are shown in table 2<sup>87</sup>. Most of the favorable values for the mixing angle however occur for  $\alpha$  values for which  $\alpha_D(M_X) > \alpha_3(M_X)$  and "E<sub>6</sub> unification" is excluded.  $SO(10) \times U(1)_D$  unification is possible for specific choices of  $\alpha_F$  and  $\alpha_D$ . It all depends of course on the particle content above  $M_X$ .

Summarizing, we have proposed and analysed an

<sup>86</sup> We introduce the normalized (for the 27 representation of E<sub>6</sub>)  $U(1)$  generators  $Z = (\sqrt{30})Z$ ,  $\tilde{X} = (\sqrt{10})\tilde{X}$ ,  $\tilde{\Omega} = \frac{1}{2}\tilde{\Omega}$  ( $\text{Tr } Z^2 = \text{Tr } \tilde{X}^2 = \text{Tr } \tilde{\Omega}^2 = 2$ ) and consequently  $\alpha_F = \frac{1}{10}\alpha_F$ ,  $\alpha_D = \frac{1}{10}\alpha_D$ ,  $\alpha_Y = \frac{1}{10}\alpha_Y$  and  $Y = \frac{1}{2}\tilde{Y} + \sqrt{\frac{3}{10}}\tilde{X} - \sqrt{\frac{1}{10}}\tilde{Z}$ . Then, according to ref. [8]  $1/\alpha_Y = \frac{2}{3}/\alpha_D + \frac{1}{10}/\alpha_F + \frac{1}{10}\alpha_Y = 1/\tilde{\alpha} + \frac{1}{10}/\alpha_Y$

<sup>87</sup> We have used  $\alpha_3 = 0.13$ ,  $\alpha = 1/128$ . We have assumed that  $M = 10^{18}$  GeV and that the mass of the intermediate scale isodoublet pair is  $M'_X/M^2$  in accordance with (17).

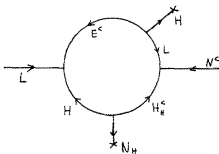


Fig. 2. Radiative neutrino mass.

Table 2  
Values for the  $\sin^2\theta_w(M_w)$ ,  $M_X$  and  $\alpha_5(M_X)$ .

$\bar{\alpha}^{-1}$	$\sin^2\theta_w$	$M_X$ (GeV)	$\alpha_5$
26	0.237	$7.30 \times 10^{16}$	$5.38 \times 10^{-2}$
28	0.234	$2.75 \times 10^{16}$	$5.47 \times 10^{-2}$
30	0.232	$1.04 \times 10^{16}$	$5.57 \times 10^{-2}$
32	0.230	$3.90 \times 10^{15}$	$5.56 \times 10^{-2}$
34	0.227	$1.47 \times 10^{15}$	$5.77 \times 10^{-2}$
36	0.225	$5.53 \times 10^{14}$	$5.87 \times 10^{-2}$
38	0.222	$2.08 \times 10^{14}$	$5.98 \times 10^{-2}$

adjointless  $SU(5) \times U(1)_X \times U(1)_D$  model which may be obtainable from a string theory and which exhibits a set of attractive properties. It has a natural triplet doublet mass splitting, it leads to phenomenologically acceptable values for  $\sin^2\theta_w$  and it predicts naturally light neutrinos.

## References

- [1] M.B. Green and J.H. Schwarz, Phys. Lett. B 149 (1984) 117;
- D.J. Gross, J.A. Harvey, E. Martinec and R. Rohm, Nucl. Phys. B 256 (1985) 468 and B 267 (1986) 75;
- P. Candelas, G.T. Horowitz, A. Strominger and E. Witten, Nucl. Phys. B 258 (1985) 46;
- E. Witten, Nucl. Phys. B 268 (1986) 79;
- L. Dixon, J.A. Harvey, C. Vafa and E. Witten, Nucl. Phys. B 261 (1985), 678 and B 274 (1986) 285.
- [2] K. Narain, Phys. Lett. 169 B (1986) 41;
- W. Lerche, D. Lüst and A.N. Schellekens, Nucl. Phys. B 287 (1987) 477;
- H. Kawai, D. Lewellen and S.H. Tye, Phys. Rev. Lett. 57 (1986) 1832; Nucl. Phys. B 288 (1987) 1.
- [3] I. Antoniadis, C. Bachas and C. Kounnas, Nucl. Phys. B 289 (1987) 87;
- I. Antoniadis and C. Bachas, Nucl. Phys. B 298 (1988) 586.
- [4] S.M. Barr, Phys. Lett. B 112 (1982) 219;
- J.P. Derendinger, J.E. Kim and D.V. Nanopoulos, Phys. Lett. B 130 (1984) 170.
- [5] I. Antoniadis, J. Ellis, J.S. Hagelin and D.V. Nanopoulos, Phys. Lett. B 194 (1987) 231;
- B.A. Campbell, J. Ellis, J.S. Hagelin, D.V. Nanopoulos and R. Ticciati, Phys. Lett. B 198 (1987) 200.
- [6] B.A. Campbell, J. Ellis, J.S. Hagelin and D.V. Nanopoulos, CERN preprint CERN-TH 4931/87.
- [7] A. Masiero, D.V. Nanopoulos and A. Sanda, Phys. Rev. Lett. 57 (1986) 663.
- [8] J.E. Kim and H.S. Song, Phys. Rev. D 22 (1980) 1753.